



Artificial Intelligence

1. Uninformed Search

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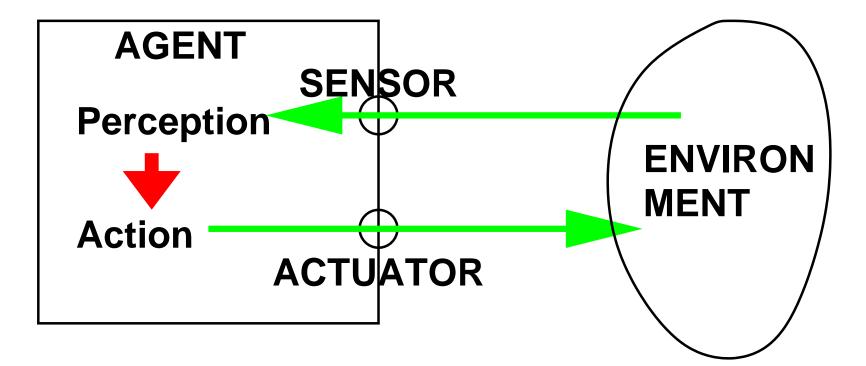


1. The Agent Metaphor

- 2. Problem Descriptions
- 3. Uninformed Tree Search
- 4. Uninformed Graph Search

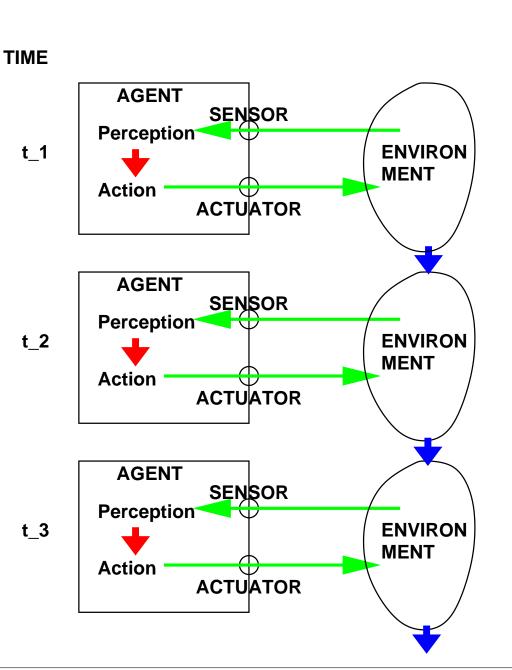
Artificial Intelligence / 1. The Agent Metaphor

Agent, Environment, Perceptions, and Actions



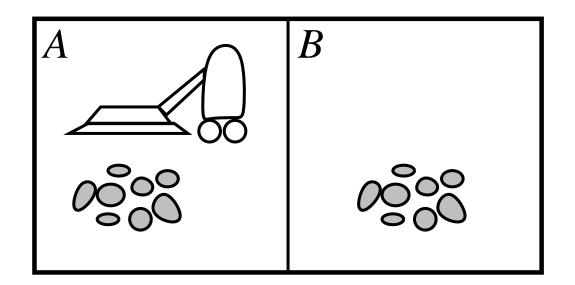


Perception Sequence and Action Sequence





Silly Example: The vacuum-cleaner world



Perceptions: pairs of

- location of the vacuum-cleaner: square A or square B
- content at that location: clean or dirty

Actions: move left, move right, suck dirt, do nothing.



Silly Example: The vacuum-cleaner world



Perception sequence	action sequence
(A, clean)	right
(A, dirty)	suck
(B, clean)	left
(B, dirty)	suck
(A, clean), (A, clean)	?

Silly Example: The vacuum-cleaner world



Perception sequence	action sequence
(A, dirty)	suck
(A, clean)	right
(B, dirty)	suck
(B, clean)	left
(A, clean), (B, clean)	noop
(B, clean), (A, clean)	noop

Components of Environments



Environements consist of four components (so-called "PEAS" model):

Performance measure:

describes successful behavior of an agent; the goal.

Environment:

describes what other entities there are to interact with.

Actuators:

describes the actions an agent can take and how they influence the environment.

Sensors:

describes the perceptions available to an agent.

Properties of Environments (1/2)



deterministic – stochastic:

deterministic: the next state is completely determined by the previous state and the action.

static – dynamic:

static: the state of the environment does not change while the agent deliberates,

e.g., a turn-based game.

fully observable – partially observable:

fully observable: all properties of the true state that are relevant to take the optimal action are perceived, e.g., in chess.

partially observable: e.g., the vacuum world with information just about the actual location.

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Properties of Environments (2/2)



discrete – continuous:

discrete time: e.g., measured in steps.

discrete states: e.g., counts; locations on a grid; etc.

discrete perceptions: e.g., counts; locations on a grid; etc.

(same as for states).

discrete actions: e.g., just steering left/right (but not by a continuous angle).

Episodic – sequential:

episodic: actions influence only the next state, but not any later states.

Single agent – multiagent:

multiagent: several agents act in the environment. (cooperative vs. competitive scenarios)



1. The Agent Metaphor

2. Problem Descriptions

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4. Uninformed Graph Search

Problems



A **problem** consists of six components (here 1–4):

super state space: set $X^{\#}$

a set of entities that describe the state of the environment, i.e., the actual configuration at a given point in time.

action space: set A

a set of entities that describe the actions that an agent may perform.

initial state: element $x_0 \in X^{\#}$

the state the agent starts in.

successor function: partial function succ : $X^{\#} \times A \rightarrow X^{\#}$

triples x, a, x' consisting of

- previous state x,

- possible action a in that state and
- follow up state x'

(for deterministic environments)

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Problems / State space

Initial states and successor function implicitly define the **state space** *X* by enumeration:

$$X := \bigcup_{n \in \mathbb{N}} \operatorname{succ}^n(x_0) \subseteq X^{\#}$$

where succⁿ denotes the *n*-th power of succ(\cdot , A), i.e.,

$$\begin{split} & \mathsf{succ}^0(x) = x, \\ & \mathsf{succ}^1(x) = \mathsf{succ}(x, A) = \bigcup_{a \in A} \mathsf{succ}(x, a), \\ & \mathsf{succ}^2(x) = \mathsf{succ}(\mathsf{succ}(x, A), A) = \bigcup_{a \in A} \bigcup_{a' \in A} \mathsf{succ}(\mathsf{succ}(x, a'), a) \text{ etc.} \end{split}$$

Obviously,

$$x_0 \in X$$

and succ can be restricted to

$$\mathsf{succ} \subseteq X \times A \times X$$



Problems



A **problem** consists of six components (here 5–6):

goal test: $g: X \to \{0, 1\}$

a function that evaluates if a given state is a goal or not.

Sometimes the set of goals $g^{-1}(1)$ is enumerated explicitly, e.g., $g^{-1}(1) = \{$ In(Bucharest) $\}$.

path costs: $c : (A \times X)^* \to \mathbb{R}$

the cost of performing the sequence of actions a_1, a_2, \ldots, a_n to move from x_0 to x_1 , from x_1 to x_2 , etc., and finally from x_{n-1} to x_n .

Path costs often are assumed to be just the sum of single step costs:

$$c(a_1, x_1, a_2, x_2, \dots, a_n, x_n) = \sum_{i=1}^n c_{\text{step}}(x_{i-1}, a_i, x_i)$$

Problems / State graph

Problems can be represented as directed graphs with labeled edges:

```
vertices: states X.
```

edges: there is an edge from vertex x to x' if there is an action a with succ(x, a) = x'.

edge labels: edges are labeled twofold:

- with the action *a* and
- with the step costs c(x, a, x').

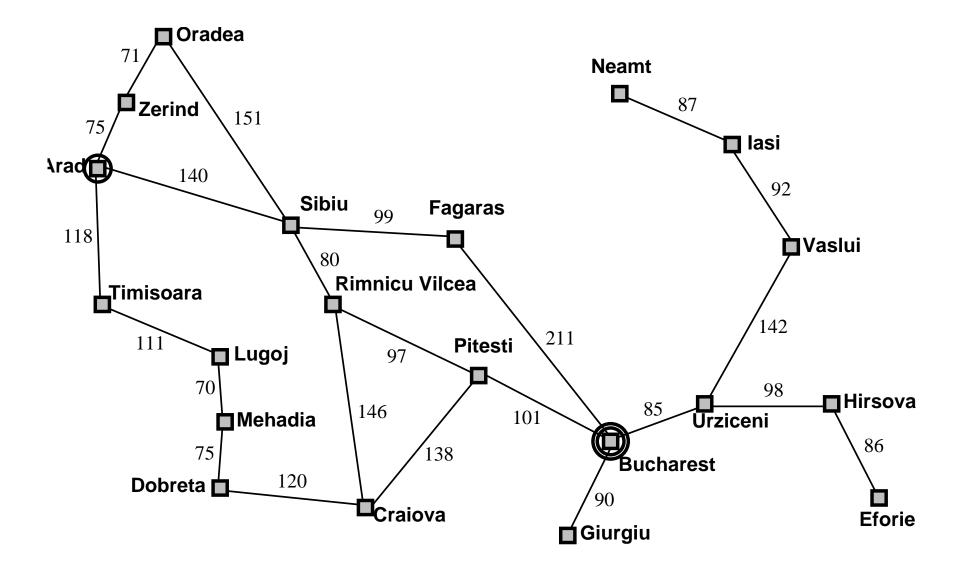
If from each state each successor state can be reached by at most one action, the action label often is omitted (as it is fully determined by the two states).



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Problems / State graph / Example





Solutions



A path in the state space can be described either by a sequence $(a_1, x_1, a_2, x_2, \ldots, a_n, x_n) \in (A \times X)^*$, with $succ(x_{i-1}, a_i) = x_i$, $i = 1, \ldots, n$

or equivalently by a pure action sequence

$$(a_1, a_2, \dots, a_n) \in A^*$$

where

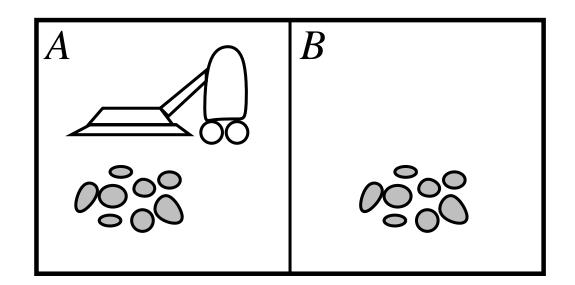
$$x_i := \operatorname{SUCC}(x_{i-1}, a_i), \quad i = 1, \dots, n$$

A solution is a path that reaches a goal, i.e., with $g(x_n) = 1$.

An **optimal solution** is a solution with smallest cost $c(a_1, x_1, a_2, x_2, ..., a_n, x_n)$ among all solutions.

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Examples / Vacuum cleaner



state space $X := \{A, B\} \times \{\text{dirty}, \text{clean}\}^{\{A, B\}}, |X| = 8.$ initial state any.

successor function

 $\mathsf{succ}((A, \{(A, \mathsf{dirty}), (B, \mathsf{dirty})\}), \mathsf{suck}) = (A, \{(A, \mathsf{clean}), (B, \mathsf{dirty})\})$

etc. (see next slide).

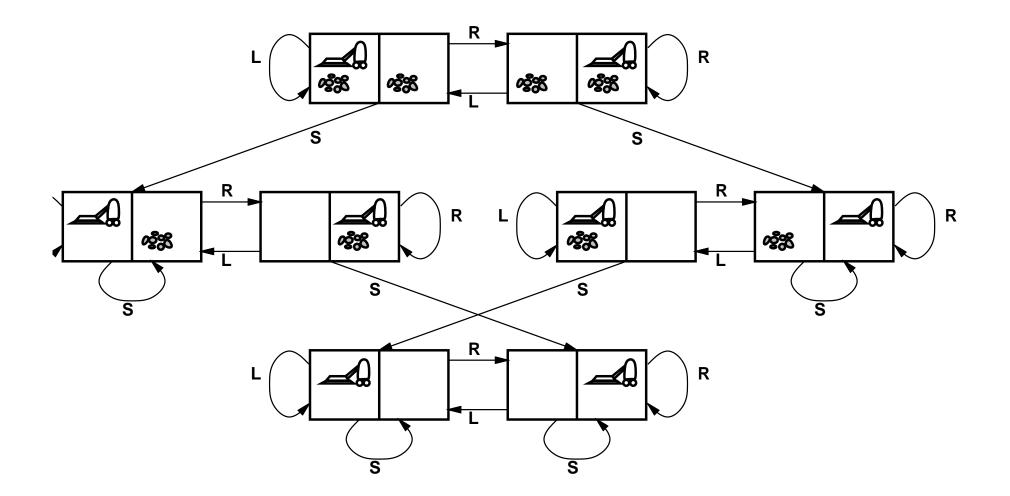
goal function: $g((*, \{(A, clean), (B, clean)\})) = 1$, else 0.

path cost: c(x, a, x') = 1



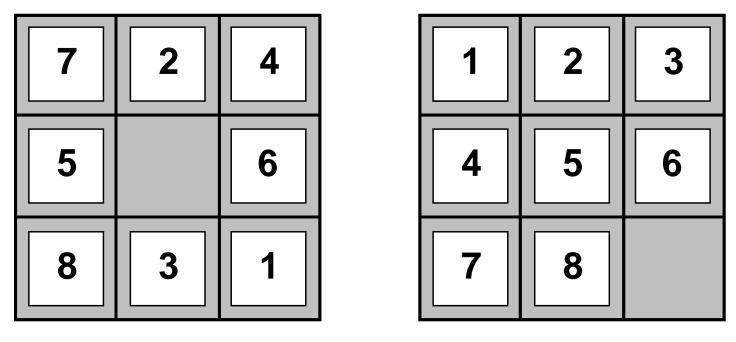
Examples / Vacuum cleaner





Examples / 8-puzzle





Start State

Goal State

state space $X := \{f : \{1, 2, \dots, 8\} \rightarrow \{1, 2, \dots, 9\} \mid f \text{ injective}\}.$ initial state any.

successor function effect of moving the blank (see next slide). **goal function:** g(designated goal state) = 1, else 0. **path cost:** c(x, a, x') = 1

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Examples / 8-puzzle



$$\operatorname{succ}\left(\begin{pmatrix} 7 & 2 & 4 \\ 5 & 6 \\ 8 & 3 & 1 \end{pmatrix}, \operatorname{move blank \, left}\right) = \begin{pmatrix} 7 & 2 & 4 \\ 5 & 6 \\ 8 & 3 & 1 \end{pmatrix}$$

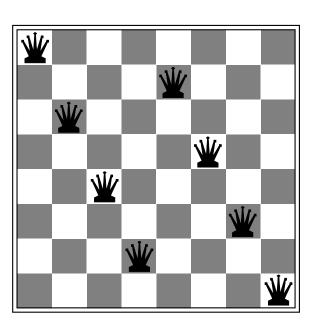
Examples / 8-puzzle



8-puzzle is an instance of the **sliding-block puzzle** class, a NP-complete problem class.

name	board	reachable states	difficulty
8-puzzle	3×3	9!/2 = 181,440	solved easily
15-puzzle	4×4	$pprox 1.3 \cdot 10^{18}$	solved in a few milliseconds
24-puzzle	5×5	$\approx 10^{25}$	difficult to solve
24-puzzle	5×5	$pprox 10^{25}$	difficult to solve

Examples / 8-queens problem



state space

$$X := \{x \subset \{1, \dots, 64\} \mid |x| \le 8\}, \quad |X| = \binom{64}{8} = 4.4 \cdot 10^9$$

initial state $x = \emptyset$.

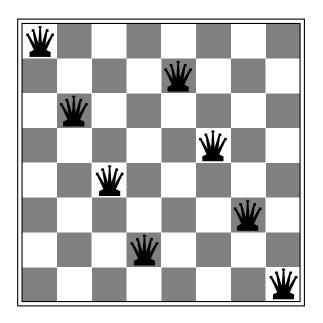
successor function add a queen to any empty square.

goal function: goal reached if 8 queens on the board, none attacked.

path cost:
$$c(x, a, x') = 1$$



Examples / 8-queens problem



A better problem formulation:

state space *n* queens (n = 0, ..., 8) in the *n* left-most columns, one per column, non attacked. |X| = 2057.

initial state $x = \emptyset$.

- **successor function** add a queen to the left-most empty column, not attacked.
- goal function: goal reached if 8 queens on the board, none attacked.

path cost: c(x, a, x') = 1





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The Problem (1/3)

Algorithmics / Graph theory:

Given a directed graph G := (V, E) with edge weights $w : E \to \mathbb{R}$ and two vertices $x, y \in V$, find a shortest path from x to y, i.e., a path $P \in V^*$ with $P_1 = x, P_n = y$ and

$$w(P) := \sum_{i=1}^{n-1} w(P_i, P_{i+1})$$

minimal among all paths from x to y.

Artificial Intelligence:

If from each state any other state can be reached by at most one action and costs decompose in single step costs, then

$$V := X \quad (\text{the states})$$

$$E := \{(x, y) \in X^2 \mid \exists a \in A : \text{succ}(x, a) = y\}$$

$$w(x, y) := \text{cost}(x, a, y) \quad (a \text{ unique with succ}(x, a) = y)$$

$$x := x_0 \quad (\text{initial state})$$

$$y := \text{any } x \in X \text{ with } g(x) = 1$$

The Problem (2/3)



But:

- X often is not finite, so it cannot be stored, but relevant portions must be constructed by succ recursively.
- $g^{-1}(1)$ may not be easy to compute (although for each specific x it may be easy to check if g(x) = 1, e.g., check-mate).

The Problem (3/3)



For this section, assume:

Each state can be reached by at most one sequence of actions.

I.e., the search space is a tree.

Breadth-First Search

Idea:

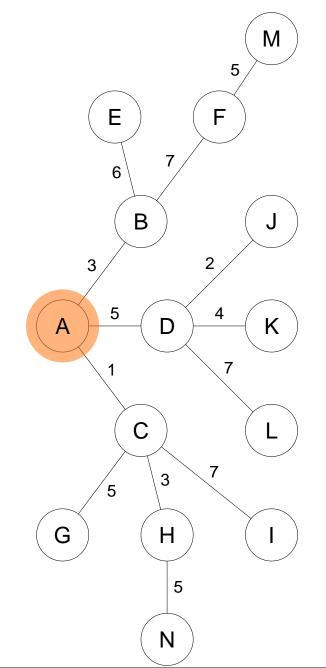
- start with initial state as border.
- iteratively replace border by all states reachable from the old border.

```
i breadth-first-search(X, succ, border, q) :
2 newborder := \emptyset
  for x \in border do
 3
        for y \in \operatorname{succ}(x, A) do
 4
            \underline{\mathbf{if}} g(y) = 1
 5
               return y
 6
             else
7
                  newborder := newborder \cup \{y\}
8
             fi
 9
        od
10
11 od
12 if newborder \neq \emptyset
      return breadth-first-search(X, succ, newborder, g)
13
14 else
         <u>return</u> Ø
15
16 fi
```



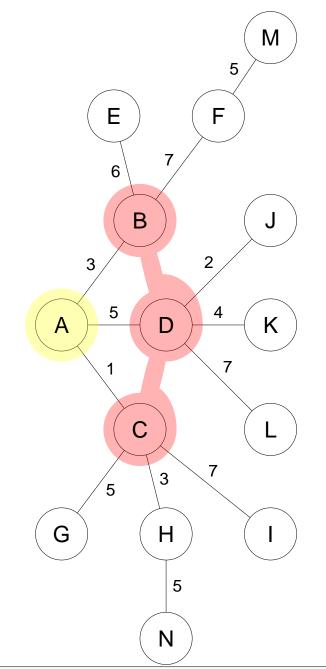
Breadth-First Search / Example





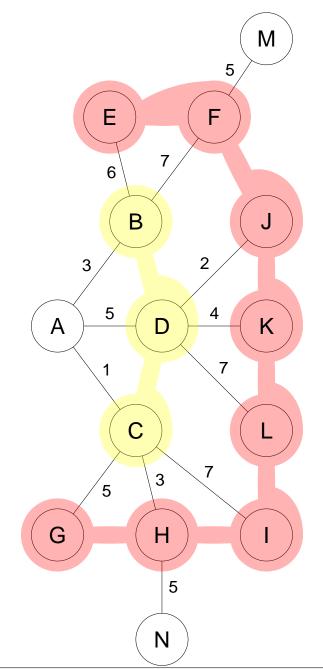
Breadth-First Search / Example





Breadth-First Search / Example





Breadth-First Search



```
i breadth-first-search(X, succ, border, g) :
 <sup>2</sup> newborder := \emptyset
   for x \in border do
 3
        for y \in \operatorname{succ}(x, A) do
 4
             \underline{\mathbf{if}} g(y) = 1
 5
                return y
 6
             else
 7
                  newborder := newborder \cup \{y\}
 8
             fi
 9
        od
10
11 od
12 if newborder \neq \emptyset
      return breadth-first-search(X, succ, newborder, g)
13
14 else
         return ∅
15
16 fi
```

```
i breadth-first-search(X, succ, x_0, g) :
 2 border := \{x_0\}
 3 <u>while</u> border \neq \emptyset <u>do</u>
           x := border[1]
 4
           if q(x) = 1
 5
             return x
 6
           fi
 7
           for y \in \operatorname{succ}(x, A) do
 8
                append(border, y);
 9
           od
10
           remove(border, x)
11
12 od
13 return Ø
```

Characteristics of Problems & Algorithms



In algorithmics, the **complexity of (shortest path) algorithms** is measured as number of steps as function of the **characteristics of the problem** measured as number of vertices and edges (big-O notation).

For problems with infinite number of vertices or edges this is not possible.

Use instead as problem characteristics:

maximum branching factor *b*:

maximum number of successors of a state.

depth of least-cost solution *d***:** length of least cost path to a goal state.

maximum depth of state space m

length of longest path, also called diameter; evtl. ∞ .

Characteristics of Problems / Example

Example 8-queens problem:

state space
$$X := \{x \in \{1, \dots, 64\} \mid |x| \le 8\}$$

 $|X| = \binom{64}{8} = 4.4 \cdot 10^9$

successor function add a queen to any empty square.

goal function: goal reached if 8 queens on the board, none attacked.

path cost: c(x, a, x') = 1

initial state $x = \emptyset$.

Problem characteristics of 8-queens:

maximum branching factor b = 64.

- depth of least-cost solution d = 8.
- maximum depth of state space m = 8.
- type of state graph: general graph.



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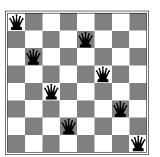
Characteristics of Problems / Example

Example 8-queens problem (better formulation):

state space n queens (n = 0, ..., 8) in the n left-most columns, one per column, non attacked.

|X| = 2057.

initial state $x = \emptyset$.



successor function add a queen to the left-most empty column, not attacked. **goal function:** goal reached if 8 queens on the board, none attacked.

path cost: c(x, a, x') = 1

Problem characteristics of 8-queens (better formulation):

```
maximum branching factor b = 8.
```

```
depth of least-cost solution d = 8.
```

```
maximum depth of state space m = 8.
```

type of state graph: tree.



Characteristics of Algorithms



Characterize by:

Completeness

does the algorithm always find a solution if one exists?

Optimality

does the algorithm always find an optimal solution?

Time complexity

size of the visited part of the search tree

Space complexity

size of the search tree in memory

Breadth-First Search



Completeness

yes (if b is finite)

Optimality

no (unless all step costs are the same, e.g., 1)

Time complexity

$$1 + b + b^2 + \dots + b^d + b(b^d - 1) = O(b^{d+1})$$

Space complexity

same as time complexity as whole search tree is kept in memory.

Uniform Cost Search

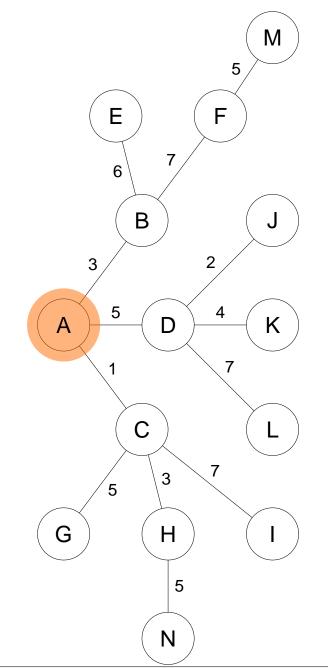
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Idea:

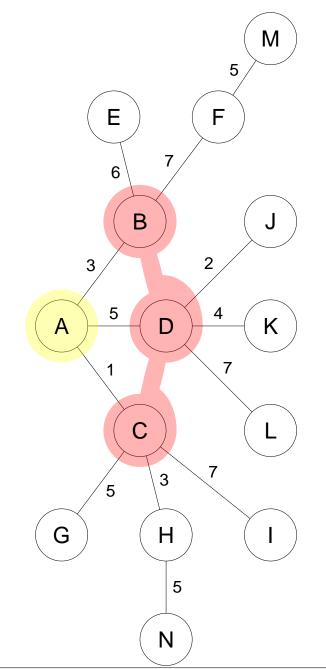
- as breadth-first search.
- but visit state with minimal path cost first.

```
i uniform-cost-search(X, succ, cost, x_0, g) :
 2 border := \{x_0\}
 s c(x_0) := 0
 4 while border \neq \emptyset do
              x := \operatorname{argmin}_{x \in \operatorname{border}} c(x)
 5
              \underline{\mathbf{if}} g(x) = 1
 6
                 return x
 7
              fi
 8
             \underline{\mathbf{for}} \ y \in \operatorname{succ}(x, A) \ \underline{\mathbf{do}}
 9
                    border := border \cup \{y\}
10
                    c(y) := c(x) + \cot(x, y)
11
              od
12
              border := border \setminus \{x\}
13
14 od
15 return ∅
```

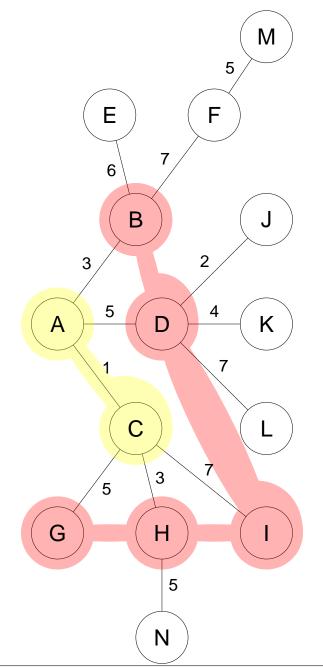




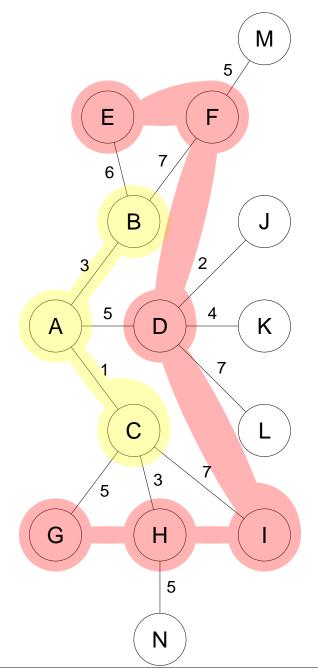




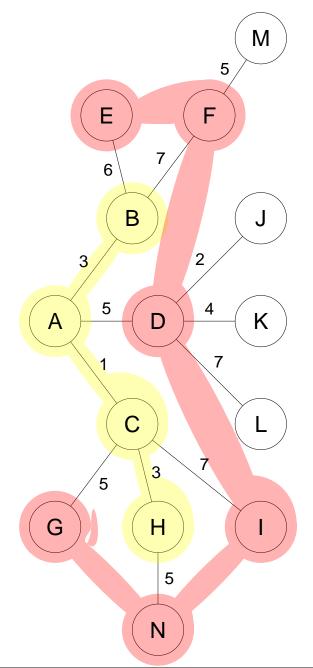












Uniform Cost Search



Completeness

yes (if step costs are $\geq \epsilon > 0$).

Optimality

yes

Time complexity

 $O(b^{1+\lfloor \frac{\operatorname{cost}(P^*)}{\epsilon} \rfloor})$, where P^* is an optimal solution.

Space complexity

same as time complexity as whole search tree is kept in memory.

Depth-First Search

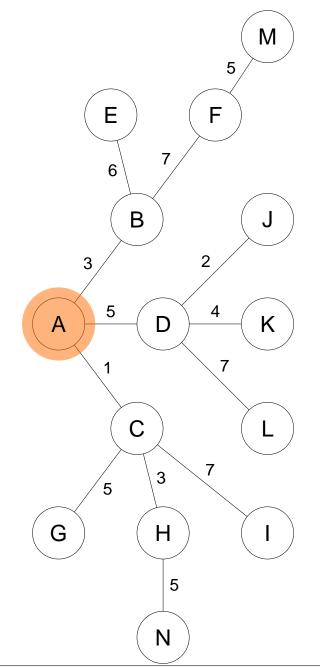


Idea:

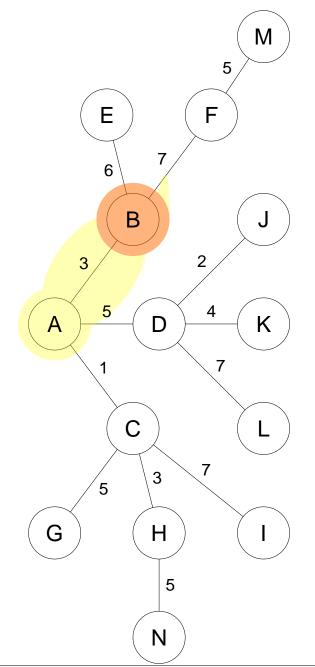
- start with initial state.
- iteratively visit successors one by one.

```
i depth-first-search(X, succ, x_0, g) :
 <sup>2</sup> for y \in \operatorname{succ}(x_0, A) do
          \underline{\mathbf{if}} g(y) = 1
 3
              return y
 4
          else
 5
                  z := \text{depth-first-search}(X, \text{succ}, y, g);
 6
                 \underline{\mathbf{if}} \ z \neq \emptyset
 7
                     return z
 8
                 fi
 9
          fi
10
11 od
12 return \emptyset
```

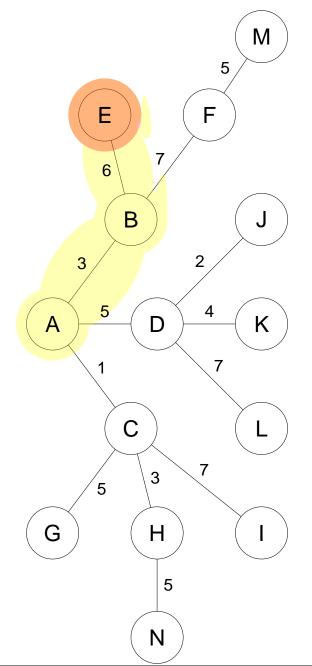




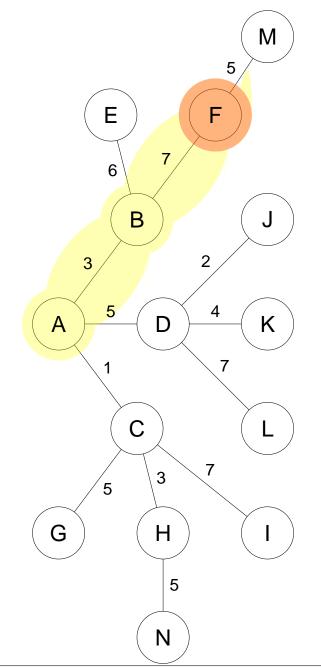




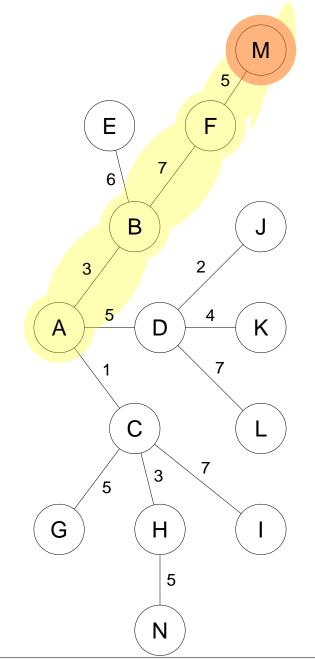




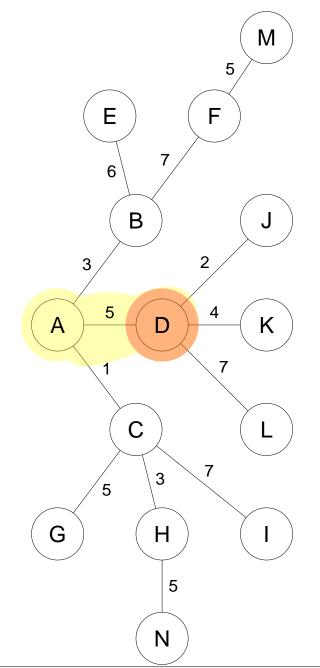




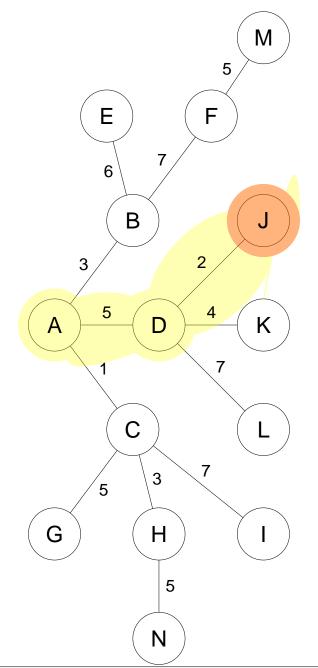












Depth-First Search



```
i depth-first-search(X, succ, x_0, g) :
 <sup>2</sup> for y \in \operatorname{succ}(x_0, A) do
           \underline{\mathbf{if}}\,g(y) = 1
 3
              return y
 4
           else
 5
                  z := \text{depth-first-search}(X, \text{succ}, y, g);
 6
                  \underline{\mathbf{if}} \ z \neq \emptyset
 7
                     return z
 8
                  fi
 9
          fi
10
11 od
12 <u>return</u> ∅
```

```
i depth-first-search(X, succ, x_0, g) :
 2 border := \{x_0\}
 <sup>3</sup> <u>while</u> border \neq \emptyset <u>do</u>
            x := border[1]
 4
            \underline{\mathbf{if}} g(x) = 1
 5
               return x
 6
            fi
 7
            for y \in \operatorname{succ}(x, A) do
 8
                 insert-at-beginning(border, y);
 9
            od
10
            remove(border, x)
11
12 od
13 return ∅
```

Depth First Search



Completeness

no (if $m = \infty$, e.g., due to loops).

Optimality

no

Time complexity

 $O(b^m)$ — bad, if m >> d, but great for dense solutions.

Space complexity

O(bm).

Depth-Limited Search

Idea:

- as depth-first search.
- stop at given maximum depth maxdepth.

```
i depth-limited-search(X, succ, x_0, g, maxdepth) :
 2 for y \in \operatorname{succ}(x_0, A) do
        \underline{\mathbf{if}}\,g(y) = 1
 3
           <u>return</u> y
 4
        elsif maxdepth > 0
 5
               z := \text{depth-limited-search}(X, \text{succ}, y, q, \text{maxdepth} - 1);
 6
               if z \neq \emptyset and z \neq "cutoff"
 7
                  <u>return</u> z
 8
               fi
 9
        fi
10
11 od
12 if maxdepth = 0
      return "cutoff"
13
14 else
         return Ø
15
16 fi
```



Depth-Limited Search



Completeness

no (if d > maxdepth).

Optimality

no

Time complexity

 $O(b^{\rm maxdepth})$

Space complexity

 $O(b \cdot \text{maxdepth}).$

Iterative Deepening Search



Idea:

- as depth-limited search.
- but repeat for increasing maximal depth maxdepth.

```
1 iterative-deepening-search(X, succ, x_0, g, maxdepth) :

2 <u>for</u> d = 1 \dots maxdepth <u>do</u>

3 P := \text{depth-limited-search}(X, \text{succ}, x_0, g, d);

4 <u>if</u> P \neq "cutoff"

5 <u>return</u> P

6 <u>fi</u>

7 <u>od</u>

8 <u>return</u> "cutoff"
```

Iterative Deepening Search



Completeness

yes

Optimality

no (unless all step costs are equal, e.g., 1; but can be modified).

Time complexity

 $O((d+1) + db + (d-1)b^2 + \ldots + b^d) = O(b^d)$

Space complexity

O(bd)

Overview



search method	Completeness	Optimality	Time complexity	Memory compl
Breadth First Search	yes ($b<\infty$)	no	$O(b^{d+1})$	$O(b^{d+1})$
		(unless $c = 1$)		
Uniform Cost Search	yes ($c \ge \epsilon$)	yes	$O(b^{1+\lfloor\frac{\operatorname{cost}(P^*)}{\epsilon}\rfloor})$	$O(b^{1+\lfloor\frac{\operatorname{cost}(P^*)}{\epsilon}\rfloor})$
Depth First Search	no (unless $m < \infty$)	no	$O(b^m)$	O(bm)
Depth-Limited Search	no (unless $d < maxdepth)$	no	$O(b^{maxdepth})$	$O(b \cdot maxdepth)$
Iterative Deepening	yes	no	$O(b^d)$	O(bd)
Search		(unless $c = 1$)		



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2. Problem Descriptions

3. Uninformed Tree Search

4. Uninformed Graph Search

Uniform Cost Search / Explicit branch bookkeeping



```
i uniform-cost-search(X, succ, cost, x_0, q) :
 2 border := \{x_0\}
 s c(x_0) := 0
 4 while border \neq \emptyset do
           x := \operatorname{argmin}_{x \in \operatorname{border}} c(x)
 5
           if q(x) = 1
 6
               return x
 7
           fi
8
           for y \in \operatorname{succ}(x, A) do
 9
                 border := border \cup \{y\}
10
                 c(y) := c(x) + \cot(x, y)
11
            od
12
            border := border \setminus \{x\}
13
14 <u>od</u>
15 return ∅
```

If succ is expensive to invert (or not possible to invert, because the search space is not a tree), branches must be stored explicitely.

```
i uniform-cost-search(X, succ, cost, x_0, q) :
 2 border := \{x_0\}
 s c(x_0) := 0
 4 <u>while</u> border \neq \emptyset <u>do</u>
            x := \operatorname{argmin}_{x \in \operatorname{border}} c(x)
 5
           if q(x) = 1
 6
              return branch(x, previous)
 7
            fi
 8
            for y \in \operatorname{succ}(x, A) do
 9
                 border := border \cup \{y\}
10
                 c(y) := c(x) + \cot(x, y)
11
                previous(y) := x
12
            od
13
            border := border \setminus \{x\}
14
15 od
16 return ∅
17
18 branch(x, previous) :
19 P := \emptyset
20 while x \neq \emptyset do
            insert-at-beginning(P, x)
21
            x := \operatorname{previous}(x)
22
23 od
24 return P
```

Uniform Cost Search / Duplicate states

If duplicate states can occur (i.e., there are several paths to the same state, i.e., the search space is not a tree), and if still a tree search should be applied, states cannot be used as index anymore, but have to be wrapped in "nodes".

The same modifications have to be applied to all other search algorithms.



Uniform Cost Search / Duplicate states



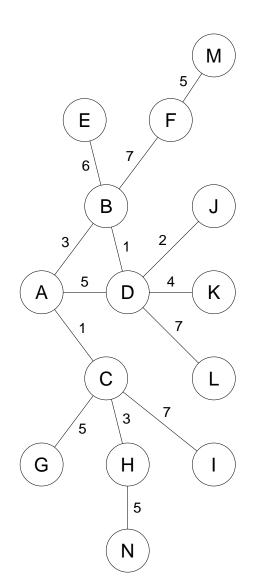
```
i uniform-cost-search(X, succ, cost, x_0, g) :
 2 border := \{x_0\}
 s c(x_0) := 0
 4 while border \neq \emptyset do
            x := \operatorname{argmin}_{x \in \operatorname{border}} c(x)
 5
            \underline{\mathbf{if}} g(x) = 1
 6
               <u>return</u> branch(x, previous)
 7
            fi
 8
            for y \in \operatorname{succ}(x, A) do
 9
                 border := border \cup \{y\}
10
                 c(y) := c(x) + \cot(x, y)
11
                 previous(y) := x
12
            od
13
            border := border \setminus \{x\}
14
15 od
16 <u>return</u> ∅
17
18 branch(x, previous) :
19 P := \emptyset
20 while x \neq \emptyset do
            insert-at-beginning(P, x)
21
            x := \operatorname{previous}(x)
22
23 od
24 return P
```

```
i uniform-cost-search(X, succ, cost, x_0, g) :
 2 N := \text{new node}(\text{state} = x_0, c = 0, \text{previous} = \emptyset)
 3 border := \{N\}
 4 while border \neq \emptyset do
             N := \operatorname{argmin}_{N \in \operatorname{border}} N.c
 5
             \underline{\mathbf{if}} g(N.\mathbf{state}) = 1
 6
                <u>return</u> branch(N)
 7
             fi
 8
             for y \in \operatorname{succ}(N.\operatorname{state}, A) do
 9
                   N' := \text{new node}(\text{state} = y)
10
                                            c = N.c + \operatorname{cost}(N.\operatorname{state}, y),
12
                                            previous := N)
14
                   border := border \cup \{N'\}
15
             od
16
             border := border \setminus \{N\}
17
18 od
19 return \emptyset
20
21 \operatorname{branch}(N) :
22 P := \emptyset
23 while N! = \emptyset do
             insert-at-beginning(P, N.state)
24
             N := N.previous
25
26 <u>od</u>
27 return P
```

Several paths blow up the search tree

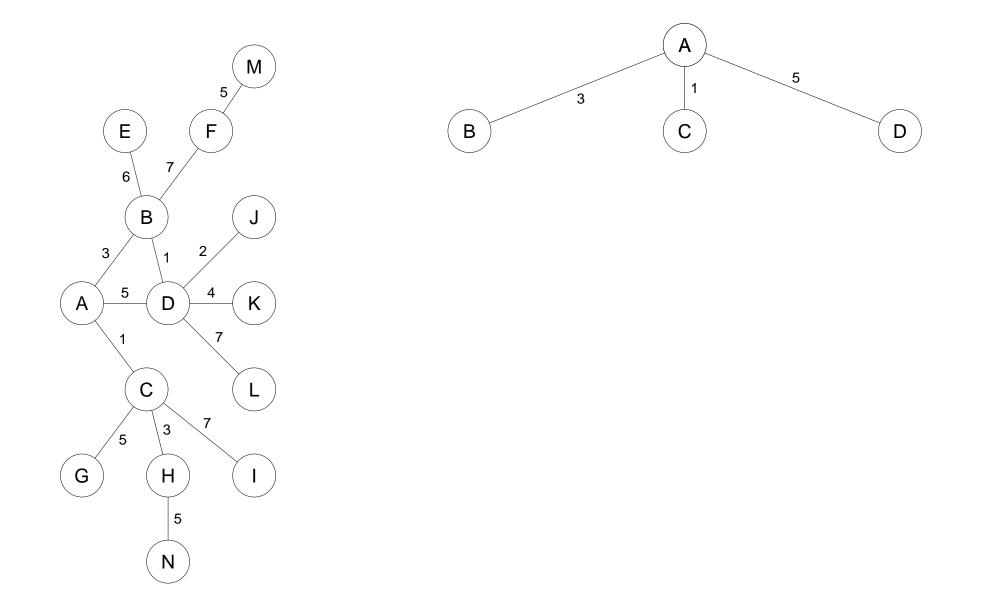


А



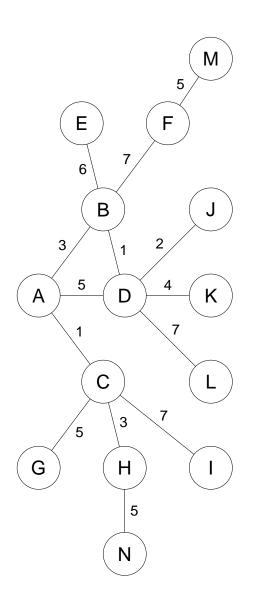
Several paths blow up the search tree

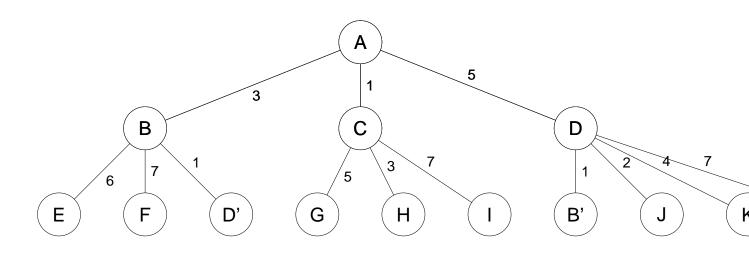




Several paths blow up the search tree







Closed list



The tree search algorithms must be modified s.t. they keep track of all the nodes visited so far (so-called **closed list**).

If the current state is already in the closed list, it is discarded instead of expanded.

This means that all algorithms have to keep the whole visited part of the state space in memory, i.e., the space complexity always is the one of breadth first search..

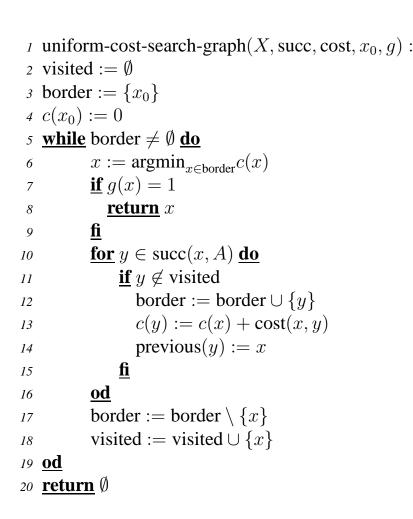
Uniform Cost Search in Graph State Spaces (1/2)



```
i uniform-cost-search(X, succ, cost, x_0, g) :
 2 border := \{x_0\}
 s c(x_0) := 0
 4 while border \neq \emptyset do
           x := \operatorname{argmin}_{x \in \operatorname{border}} c(x)
 5
           if q(x) = 1
 6
 7
              return x
            fi
8
           for y \in \operatorname{succ}(x, A) do
9
                border := border \cup \{y\}
10
                c(y) := c(x) + \cot(x, y)
11
           od
12
           border := border \setminus \{x\}
13
14 od
15 return ∅
```

i uniform-cost-search-graph(X, succ, cost, x_0, g) : 2 visited := \emptyset *3* border := $\{x_0\}$ $4 c(x_0) := 0$ 5 while border $\neq \emptyset$ do $x := \operatorname{argmin}_{x \in \operatorname{border}} c(x)$ 6 **if** q(x) = 17 return x 8 fi 9 for $y \in \operatorname{succ}(x, A)$ do 10 $\underline{\mathbf{if}} y \not\in \mathbf{visited}$ 11 border := border $\cup \{y\}$ 12 $c(y) := c(x) + \cot(x, y)$ 13 previous(y) := x14 fi 15 od 16 border := border $\setminus \{x\}$ 17 visited := visited $\cup \{x\}$ 18 19 **od** 20 <u>retu</u>rn ∅

Uniform Cost Search in Graph State Spaces (2/2)



i uniform-cost-search-graph(X, succ, cost, x_0, g) : 2 notvisited := X $s \ c(x) := \begin{cases} 0, & \text{if } x = x_0 \\ \infty, & \text{else} \end{cases}$ 4 **<u>while</u>** notvisited $\neq \emptyset$ **<u>do</u>** $x := \operatorname{argmin}_{x \in \operatorname{notvisited}} c(x)$ 5 $\underline{\mathbf{if}} g(x) = 1$ 6 return x 7 fi 8 for $y \in \operatorname{succ}(x, A)$ do 9 $c(y) := c(x) + \cot(x, y)$ 10 previous(y) := x11 od 12 notvisited := notvisited $\setminus \{x\}$ 13 14 **od** *15* return ∅





Summary (1/3) – The Agent Metaphor

- The agent metaphor describes intelligent systems as agents acting in an environment perceived through sensors and remembered as perception sequences from which an action sequence is derived that is executed with actuators.
 Performance measures describe how successful an agent behaves.
- Action tables can describe simple reactive agent behavior.
- Environments can be characterized along many characteristics such as deterministic-stochastic, static-dynamic, fully-partially observable, discrete-continuous. episodic-sequential, single-multi agent.

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Summary (2/3) – Search Problems

- More formally, many AI problems can be described as finding a path in a graph with lowest cost where often (i) the graph is not finite but generated by a successor function and (ii) the goal states are not enumerated explicitly but characterized by a goal test.
- The same problem can be represented more or less nicely as a formal search problem (see 8 queens example).
- The complexity of search problems can be described by the **maximum branching factor**, **depth of least-cost solution** and **maximum depth of state space**, and the (runtime and memory) complexity of search algorithms as function in these characteristics.
- Furthermore algorithms can be characterized by **completeness** and **optimality**.



Summary (3/3) – Uninformed Search Algorithms

- Breadth-First Search is complete and can be modified to be optimal (Uniform Cost Search). Depth First Search is not complete, but can be modified to be complete (Iterative Deepending Search). BFS suffers from memory complexity, while DFS suffers from time complexity.
- If the search space is not a tree, but a general graph, a **closed list** of all already visited states needs to be maintained.