



# Artificial Intelligence

#### 1. Uninformed Search

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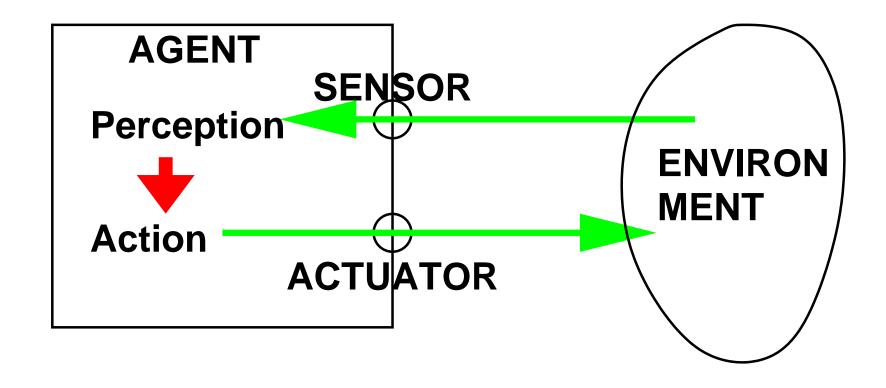
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- 1. The Agent Metaphor
- 2. Problem Descriptions
- 3. Uninformed Tree Search
- 4. Uninformed Graph Search

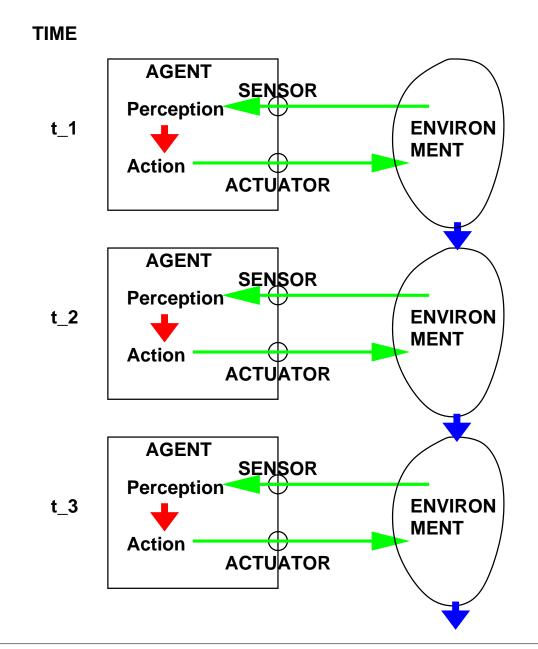


## Agent, Environment, Perceptions, and Actions



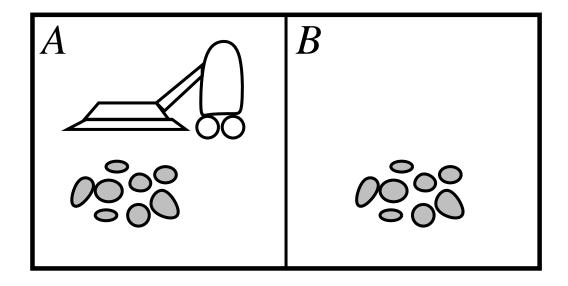


## Perception Sequence and Action Sequence





## Silly Example: The vacuum-cleaner world



Perceptions: pairs of

- location of the vacuum-cleaner: square A or square B
- content at that location: clean or dirty

Actions: move left, move right, suck dirt, do nothing.



# Silly Example: The vacuum-cleaner world

Perception sequence	action sequence
(A, clean)	right
(A, dirty)	suck
(B, clean)	left
(B, dirty)	suck
(A, clean), (A, clean)	?



## Silly Example: The vacuum-cleaner world

Perception sequence	action sequence
(A, dirty)	suck
(A, clean)	right
(B, dirty)	suck
(B, clean)	left
(A, clean), (B, clean)	noop
(B, clean), (A, clean)	noop



## Components of Environments

Environements consist of four components (so-called "PEAS" model):

#### Performance measure:

describes successful behavior of an agent; the goal.

#### **Environment:**

describes what other entities there are to interact with.

#### **Actuators:**

describes the actions an agent can take and how they influence the environment.

#### **Sensors:**

describes the perceptions available to an agent.



## Properties of Environments (1/2)

#### deterministic - stochastic:

deterministic: the next state is completely determined by the previous state and the action.

#### static – dynamic:

static: the state of the environment does not change while the agent deliberates, e.g., a turn-based game.

#### fully observable – partially observable:

fully observable: all properties of the true state that are relevant to take the optimal action are perceived, e.g., in chess.

partially observable: e.g., the vacuum world with information just about the actual location.



## Properties of Environments (2/2)

#### discrete – continuous:

discrete time: e.g., measured in steps.

discrete states: e.g., counts; locations on a grid; etc.

discrete perceptions: e.g., counts; locations on a grid; etc.

(same as for states).

discrete actions: e.g., just steering left/right (but not by a continuous angle).

## **Episodic – sequential:**

episodic: actions influence only the next state, but not any later states.

## Single agent – multiagent:

multiagent: several agents act in the environment. (cooperative vs. competitive scenarios)



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#### **Problems**

A **problem** consists of six components (here 1–4):

super state space: set  $X^{\#}$ 

a set of entities that describe the state of the environment, i.e., the actual configuration at a given point in time.

action space: set A

a set of entities that describe the actions that an agent may perform.

initial state: element  $x_0 \in X^{\#}$  the state the agent starts in.

**successor function:** partial function succ :  $X^{\#} \times A \rightarrow X^{\#}$  triples x, a, x' consisting of

- previous state x,
- possible action a in that state and
- follow up state x'

(for deterministic environments)

# John Soos

#### Problems / State space

Initial states and successor function implicitly define the **state** space X by enumeration:

$$X := \bigcup_{n \in \mathbb{N}} \operatorname{succ}^n(x_0) \subseteq X^{\#}$$

where succ<sup>n</sup> denotes the n-th power of succ $(\cdot, A)$ , i.e.,

$$\begin{aligned} &\operatorname{succ}^0(x) = x, \\ &\operatorname{succ}^1(x) = \operatorname{succ}(x,A) = \bigcup_{a \in A} \operatorname{succ}(x,a), \\ &\operatorname{succ}^2(x) = \operatorname{succ}(\operatorname{succ}(x,A),A) = \bigcup_{a \in A} \bigcup_{a' \in A} \operatorname{succ}(\operatorname{succ}(x,a'),a) \text{ etc.} \end{aligned}$$

Obviously,

$$x_0 \in X$$

and succ can be restricted to

$$succ \subseteq X \times A \times X$$



#### **Problems**

A **problem** consists of six components (here 5–6):

goal test:  $g: X \rightarrow \{0, 1\}$ 

a function that evaluates if a given state is a goal or not.

Sometimes the set of goals  $g^{-1}(1)$  is enumerated explicitely, e.g.,  $g^{-1}(1) = \{\text{In(Bucharest)}\}.$ 

path costs:  $c: (A \times X)^* \to \mathbb{R}$ 

the cost of performing the sequence of actions  $a_1, a_2, \ldots, a_n$  to move from  $x_0$  to  $x_1$ , from  $x_1$  to  $x_2$ , etc., and finally from  $x_{n-1}$  to  $x_n$ .

Path costs often are assumed to be just the sum of single step costs:

$$c(a_1, x_1, a_2, x_2, \dots, a_n, x_n) = \sum_{i=1}^n c_{\mathsf{step}}(x_{i-1}, a_i, x_i)$$



#### Problems / State graph

Problems can be represented as directed graphs with labeled edges:

**vertices:** states X.

**edges:** there is an edge from vertex x to x' if there is an action a with succ(x, a) = x'.

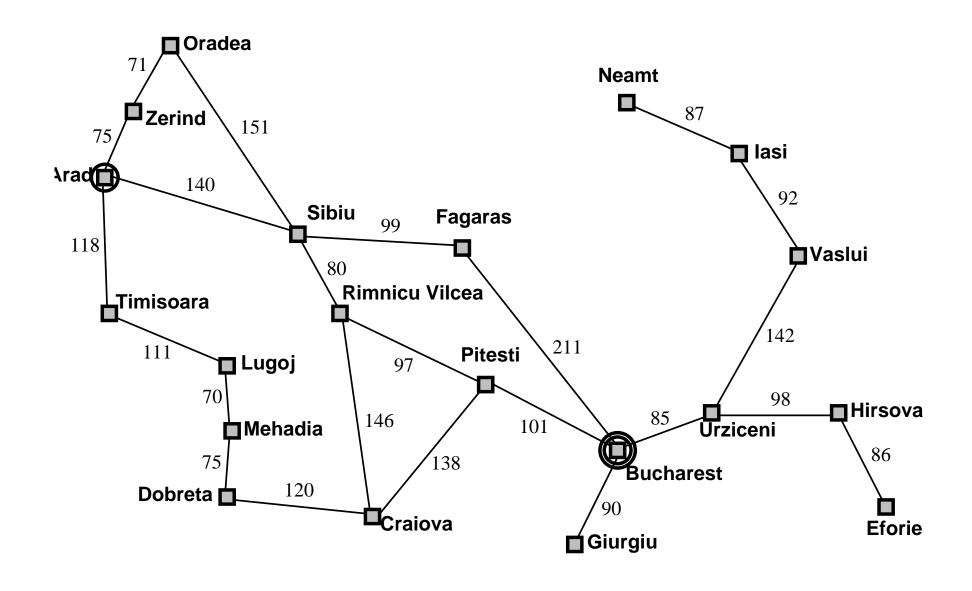
edge labels: edges are labeled twofold:

- with the action a and
- with the step costs c(x, a, x').

If from each state each successor state can be reached by at most one action, the action label often is omitted (as it is fully determined by the two states).



#### Problems / State graph / Example





#### Solutions

A path in the state space can be described either by a sequence

$$(a_1, x_1, a_2, x_2, \dots, a_n, x_n) \in (A \times X)^*, \text{ with } succ(x_{i-1}, a_i) = x_i, i = 1, \dots, n$$

or equivalently by a pure action sequence

$$(a_1, a_2, \dots, a_n) \in A^*$$

where

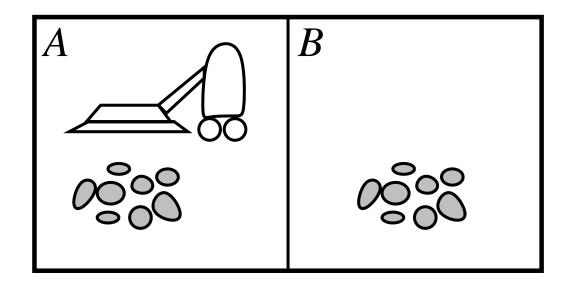
$$x_i := \mathtt{SUCC}(x_{i-1}, a_i), \quad i = 1, \dots, n$$

A **solution** is a path that reaches a goal, i.e., with  $g(x_n) = 1$ .

An **optimal solution** is a solution with smallest cost  $c(a_1, x_1, a_2, x_2, \dots, a_n, x_n)$  among all solutions.



#### Examples / Vacuum cleaner



state space  $X := \{A, B\} \times \{\text{dirty}, \text{clean}\}^{\{A, B\}}, \quad |X| = 8.$  initial state any.

#### successor function

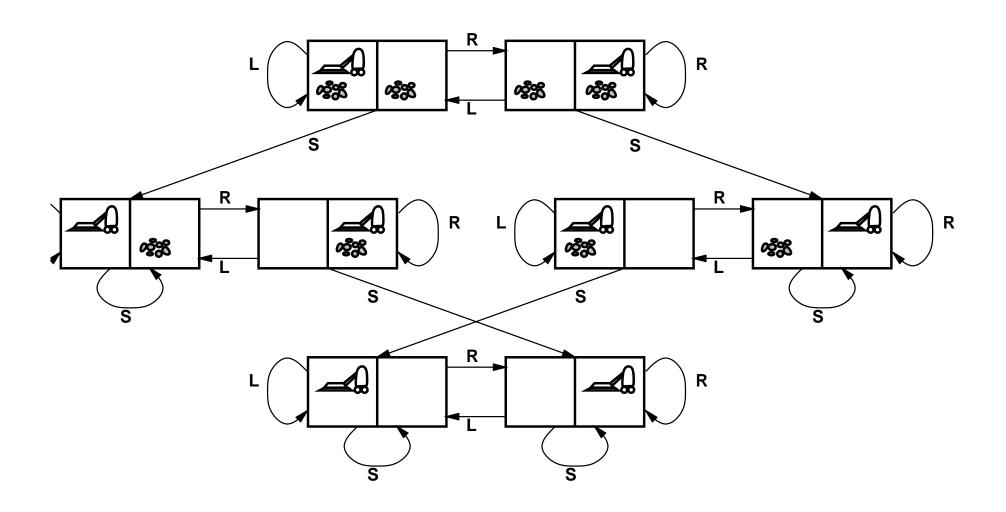
 $succ((A, \{(A, dirty), (B, dirty)\}), suck) = (A, \{(A, clean), (B, dirty)\})$  etc. (see next slide).

**goal function:**  $g((*, \{(A, clean), (B, clean)\})) = 1$ , else 0.

path cost: c(x, a, x') = 1

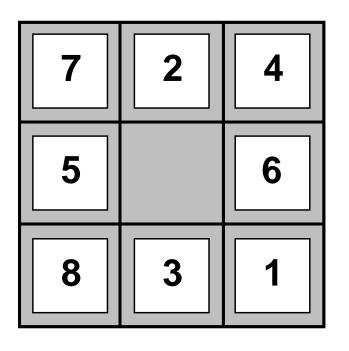


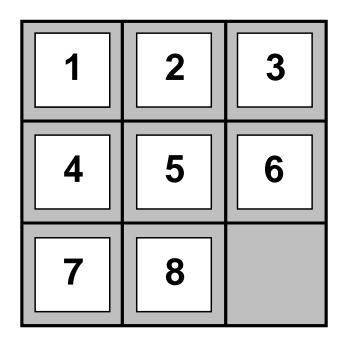
## Examples / Vacuum cleaner





#### Examples / 8-puzzle





**Start State** 

**Goal State** 

state space  $X := \{f : \{1, 2, \dots, 8\} \rightarrow \{1, 2, \dots, 9\} \mid f \text{ injective}\}.$  initial state any.

successor function effect of moving the blank (see next slide).

**goal function:** g(designated goal state) = 1, else 0.

path cost: c(x, a, x') = 1



## Examples / 8-puzzle

$$\mathbf{succ}(\begin{pmatrix} 7 & 2 & 4 \\ 5 & 6 \\ 8 & 3 & 1 \end{pmatrix}, \mathbf{move\ blank\ left}) = \begin{pmatrix} 7 & 2 & 4 \\ 5 & 6 \\ 8 & 3 & 1 \end{pmatrix}$$



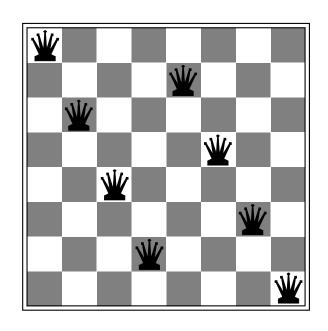
## Examples / 8-puzzle

8-puzzle is an instance of the **sliding-block puzzle** class, a NP-complete problem class.

name	board	reachable states	difficulty
8-puzzle	$3 \times 3$	9!/2 = 181,440	solved easily
15-puzzle	$4 \times 4$	$\approx 1.3 \cdot 10^{18}$	solved in a few milliseconds
24-puzzle	$5 \times 5$	$\approx 10^{25}$	difficult to solve



#### Examples / 8-queens problem



#### state space

$$X := \{x \subset \{1, \dots, 64\} \mid |x| \le 8\}, \quad |X| = \binom{64}{8} = 4.4 \cdot 10^9$$

initial state  $x = \emptyset$ .

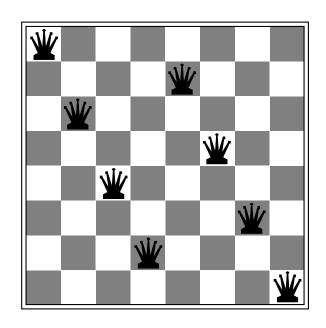
successor function add a queen to any empty square.

**goal function:** goal reached if 8 queens on the board, none attacked.

path cost: c(x, a, x') = 1



#### Examples / 8-queens problem



A better problem formulation:

**state space** n queens (n = 0, ..., 8) in the n left-most columns, one per column, non attacked. |X| = 2057.

initial state  $x = \emptyset$ .

**successor function** add a queen to the left-most empty column, not attacked.

**goal function:** goal reached if 8 queens on the board, none attacked.

path cost: c(x, a, x') = 1



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#### The Problem (1/3)

#### Algorithmics / Graph theory:

Given a directed graph G:=(V,E) with edge weights  $w:E\to\mathbb{R}$  and two vertices  $x,y\in V$ , find a shortest path from x to y, i.e., a path  $P\in V^*$  with  $P_1=x,P_n=y$  and

$$w(P) := \sum_{i=1}^{n-1} w(P_i, P_{i+1})$$

minimal among all paths from x to y.

#### Artificial Intelligence:

If from each state any other state can be reached by at most one action and costs decompose in single step costs, then

$$\begin{array}{l} V:=&X \quad \text{(the states)} \\ E:=&\{(x,y)\in X^2\,|\,\exists a\in A: \mathsf{succ}(x,a)=y\} \\ w(x,y):=&\mathsf{cost}(x,a,y) \quad (a \text{ unique with } \mathsf{succ}(x,a)=y) \\ x:=&x_0 \quad \text{(initial state)} \\ y:=&\mathsf{any} \ x\in X \text{ with } g(x)=1 \end{array}$$



#### The Problem (2/3)

#### But:

- *X* often is not finite, so it cannot be stored, but relevant portions must be constructed by succ recursively.
- $g^{-1}(1)$  may not be easy to compute (although for each specific x it may be easy to check if g(x) = 1, e.g., check-mate).



## The Problem (3/3)

For this section, assume:

Each state can be reached by at most one sequence of actions.

I.e., the search space is a tree.



#### **Breadth-First Search**

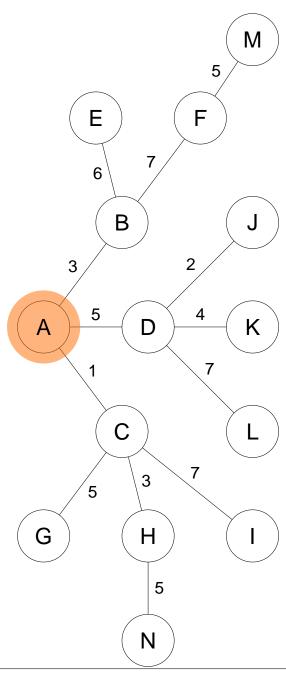
#### Idea:

- start with initial state as border.
- iteratively replace border by all states reachable from the old border.

```
1 breadth-first-search(X, succ, border, g):
2 newborder := \emptyset
  for x \in \text{border do}
       for y \in succ(x, A) do
            \mathbf{\underline{if}} g(y) = 1
               return y
            else
                 newborder := newborder \cup \{y\}
            fi
       od
10
11 od
12 if newborder \neq \emptyset
     return breadth-first-search (X, succ, newborder, g)
13
14 else
        return Ø
15
16 fi
```

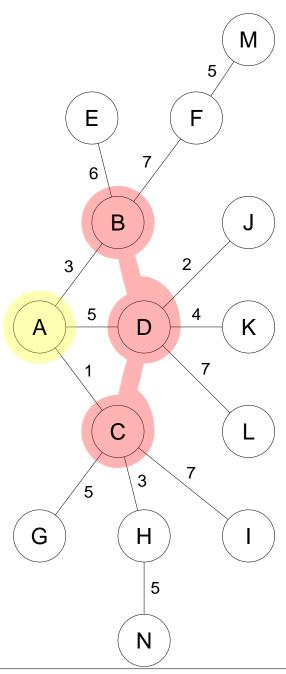


## Breadth-First Search / Example



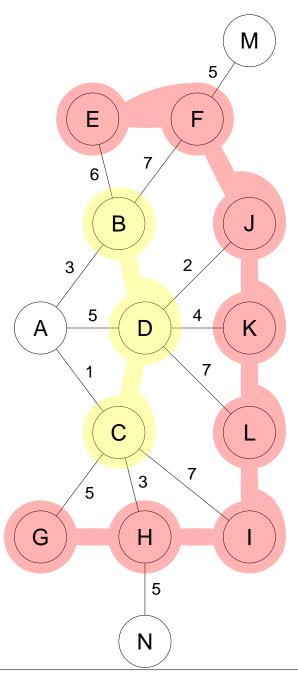


## Breadth-First Search / Example





## Breadth-First Search / Example





#### **Breadth-First Search**

```
1 breadth-first-search(X, succ, border, g):
 2 newborder := \emptyset
   for x \in \text{border do}
         \underline{\mathbf{for}}\ y \in \mathrm{succ}(x,A)\ \underline{\mathbf{do}}
              \underline{\mathbf{if}} g(y) = 1
 5
                 return y
              else
                    newborder := newborder \cup \{y\}
 8
              <u>fi</u>
 9
         od
10
11 od
12 if newborder \neq \emptyset
       return breadth-first-search(X, succ, newborder, g)
14 else
          return Ø
15
16 fi
```

```
1 breadth-first-search(X, succ, x_0, g):
 2 border := \{x_0\}
 3 while border \neq \emptyset do
          x := border[1]
          if q(x) = 1
 5
             return x
          for y \in \operatorname{succ}(x, A) do
 8
               append(border, y);
 9
          od
10
          remove(border, x)
11
12 od
13 return ∅
```



## Characteristics of Problems & Algorithms

In algorithmics, the **complexity of (shortest path) algorithms** is measured as number of steps as function of the **characteristics of the problem** measured as number of vertices and edges (big-O notation).

For problems with infinite number of vertices or edges this is not possible.

Use instead as problem characteristics:

## maximum branching factor b:

maximum number of successors of a state.

#### depth of least-cost solution d:

length of least cost path to a goal state.

#### maximum depth of state space m

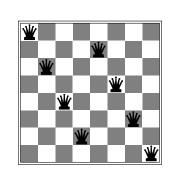
length of longest path, also called diameter; evtl.  $\infty$ .

# orsitär Allideshell 2003

## Characteristics of Problems / Example

#### Example 8-queens problem:

state space 
$$X := \{x \subset \{1, \dots, 64\} \mid |x| \le 8\}$$
  
 $|X| = \binom{64}{8} = 4.4 \cdot 10^9$ 



initial state  $x = \emptyset$ .

**successor function** add a queen to any empty square.

goal function: goal reached if 8 queens on the board, none attacked.

path cost: c(x, a, x') = 1

Problem characteristics of 8-queens:

maximum branching factor b = 64.

depth of least-cost solution d = 8.

maximum depth of state space m = 8.

type of state graph: general graph.



## Characteristics of Problems / Example

Example 8-queens problem (better formulation):

**state space** n queens (n = 0, ..., 8) in the n left-most columns, one per column, non attacked.

$$|X| = 2057.$$

initial state  $x = \emptyset$ .

successor function add a queen to the left-most empty column, not attacked.

goal function: goal reached if 8 queens on the board, none attacked.

path cost: c(x, a, x') = 1

Problem characteristics of 8-queens (better formulation):

maximum branching factor b = 8.

depth of least-cost solution d = 8.

maximum depth of state space m = 8.

type of state graph: tree.



#### Characteristics of Algorithms

#### Characterize by:

#### **Completeness**

does the algorithm always find a solution if one exists?

#### **Optimality**

does the algorithm always find an optimal solution?

#### Time complexity

size of the visited part of the search tree

#### **Space complexity**

size of the search tree in memory



#### **Breadth-First Search**

#### Completeness

yes (if b is finite)

#### **Optimality**

no (unless all step costs are the same, e.g., 1)

## **Time complexity**

$$1 + b + b^2 + \dots + b^d + b(b^d - 1) = O(b^{d+1})$$

### **Space complexity**

same as time complexity as whole search tree is kept in memory.



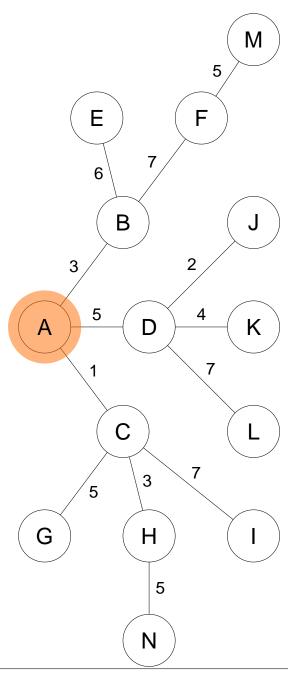
#### **Uniform Cost Search**

#### Idea:

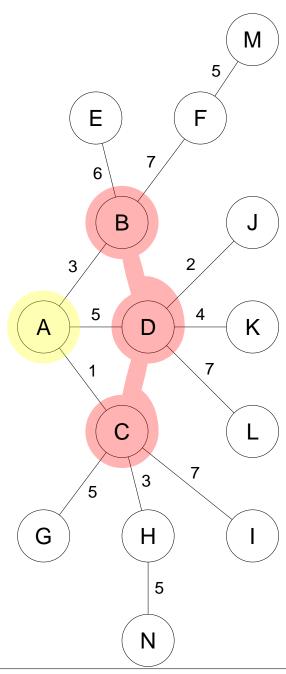
- as breadth-first search.
- but visit state with minimal path cost first.

```
i uniform-cost-search(X, succ, cost, x_0, g):
 2 border := \{x_0\}
 c(x_0) := 0
 4 while border \neq \emptyset do
             x := \operatorname{argmin}_{x \in \operatorname{border}} c(x)
             \mathbf{if} g(x) = 1
                return x
             fi
 8
             \underline{\mathbf{for}}\ y \in \mathrm{succ}(x,A)\ \underline{\mathbf{do}}
                  border := border \cup \{y\}
10
                  c(y) := c(x) + \cot(x, y)
11
             od
12
             border := border \setminus \{x\}
13
14 od
15 return ∅
```

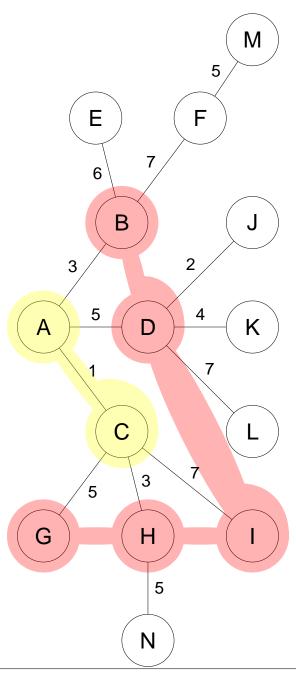




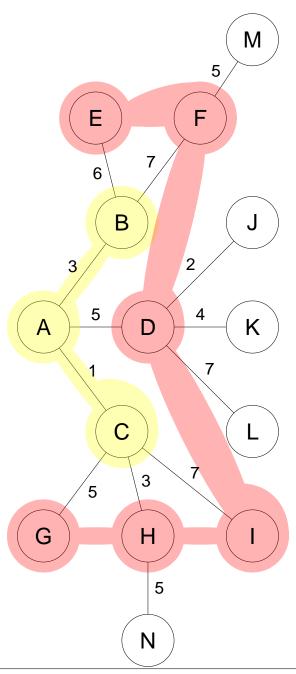




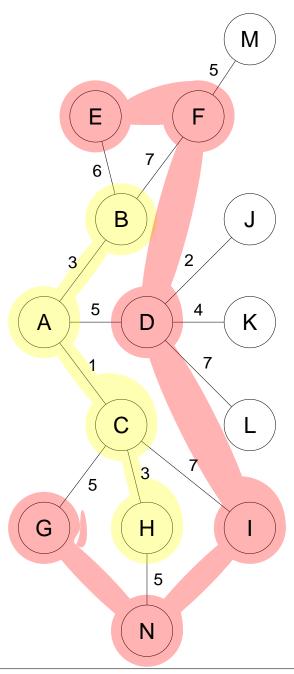














#### **Uniform Cost Search**

#### Completeness

yes (if step costs are  $\geq \epsilon > 0$ ).

#### **Optimality**

yes

## Time complexity

 $O(b^{1+\lfloor \frac{\cos t(P^*)}{\epsilon} \rfloor})$ , where  $P^*$  is an optimal solution.

#### **Space complexity**

same as time complexity as whole search tree is kept in memory.



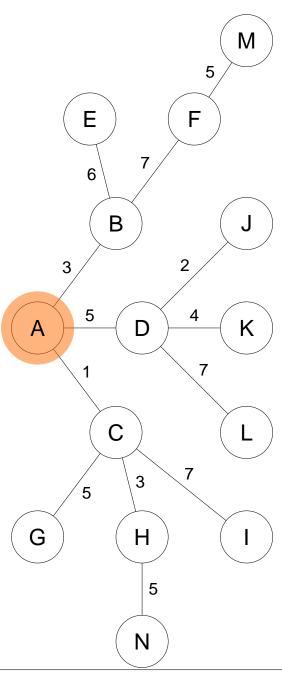
#### Depth-First Search

#### Idea:

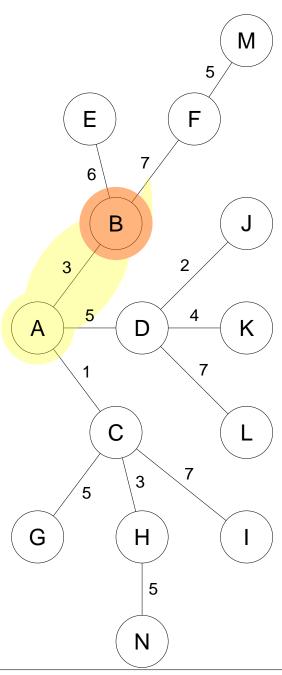
- start with initial state.
- iteratively visit successors one by one.

```
1 depth-first-search(X, succ, x_0, g):
z \text{ for } y \in \operatorname{succ}(x_0, A) \text{ do}
         \mathbf{if} g(y) = 1
            return y
         <u>else</u>
 5
                z := depth-first-search(X, succ, y, g);
 6
                \underline{\mathbf{if}} z \neq \emptyset
                   return z
 8
                fi
         fi
10
11 od
return ∅
```

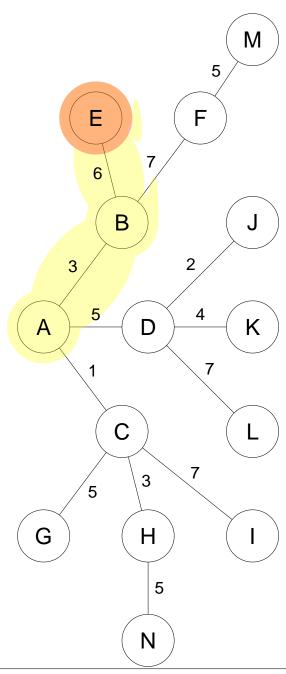




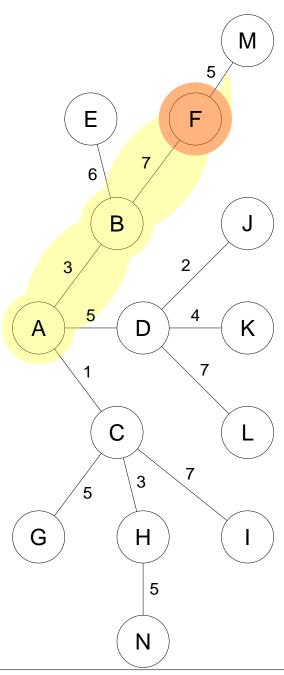




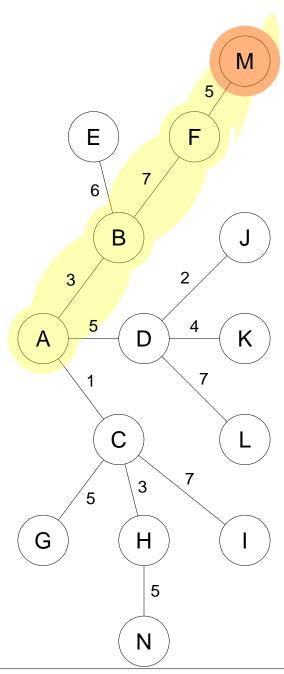




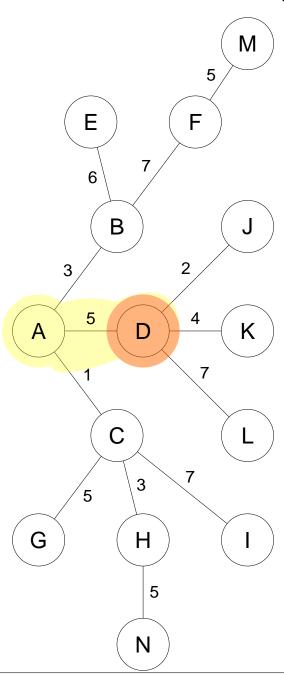




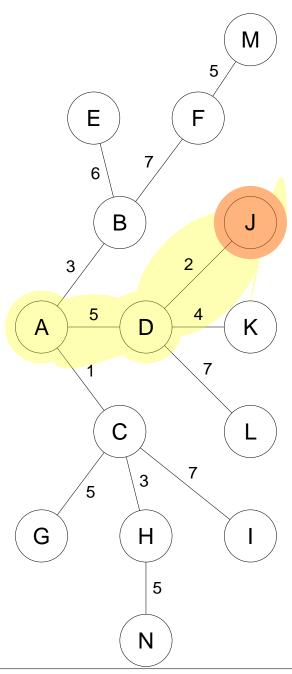














#### Depth-First Search

```
1 depth-first-search(X, succ, x_0, g):
                                                                                          i depth-first-search(X, succ, x_0, g):
 2 for y \in \operatorname{succ}(x_0, A) do
                                                                                          2 border := \{x_0\}

3
 while border ≠ 
 do
        \underline{\mathbf{if}} g(y) = 1
 3
                                                                                                    x := border[1]
           return y
 4
                                                                                                    \underline{\mathbf{if}} g(x) = 1
        else
 5
              z := depth-first-search(X, succ, y, g);
                                                                                                       return x
 6
              \underline{\mathbf{if}} z \neq \emptyset
 7
                                                                                                    for y \in succ(x, A) do
                 return z
 8
                                                                                          8
                                                                                                         insert-at-beginning(border, y);
              fi
 9
        fi
                                                                                                    od
10
                                                                                         10
                                                                                                    remove(border, x)
11 od
                                                                                         11
12 <u>return</u> ∅
                                                                                        12 od
                                                                                        13 return ∅
```



#### Depth First Search

## **Completeness**

no (if  $m = \infty$ , e.g., due to loops).

## **Optimality**

no

#### **Time complexity**

 $O(b^m)$  — bad, if m >> d, but great for dense solutions.

## **Space complexity**

$$O(bm)$$
.



### **Depth-Limited Search**

#### Idea:

- as depth-first search.
- stop at given maximum depth maxdepth.

```
I depth-limited-search(X, succ, x_0, g, maxdepth):
 2 for y \in \operatorname{succ}(x_0, A) do
        \underline{\mathbf{if}} g(y) = 1
           <u>return</u> y
        elsif maxdepth > 0
               z := \text{depth-limited-search}(X, \text{succ}, y, q, \text{maxdepth} - 1);
               if z \neq \emptyset and z \neq "cutoff"
                  <u>return</u> z
 8
               fi
 9
        <u>fi</u>
10
11 od
12 if maxdepth = 0
      return "cutoff"
14 else
         return Ø
15
16 fi
```



### **Depth-Limited Search**

#### **Completeness**

no (if d > maxdepth).

## **Optimality**

no

## **Time complexity**

 $O(b^{\mathsf{maxdepth}})$ 

## **Space complexity**

 $O(b \cdot \mathsf{maxdepth})$ .



## Iterative Deepening Search

#### Idea:

- as depth-limited search.
- but repeat for increasing maximal depth maxdepth.

```
iterative-deepening-search(X, succ, x_0, g, maxdepth):

for d = 1 \dots maxdepth do

P := \text{depth-limited-search}(X, \text{succ}, x_0, g, d);

for P \neq \text{"cutoff"}

for P \neq \text{"c
```



## Iterative Deepening Search

#### **Completeness**

yes

#### **Optimality**

no (unless all step costs are equal, e.g., 1; but can be modified).

## **Time complexity**

$$O((d+1) + db + (d-1)b^2 + \ldots + b^d) = O(b^d)$$

## **Space complexity**



# Overview

search method	Completeness	Optimality	Time complexity	Memory comple
Breadth First Search	yes $(b < \infty)$	no	$O(b^{d+1})$	$O(b^{d+1})$
		(unless $c=1$ )		
Uniform Cost Search	yes $(c \ge \epsilon)$	yes	$O(b^{1+\lfloor \frac{cost(P^*)}{\epsilon} \rfloor})$	$O(b^{1+\lfloor rac{cost(P^*)}{\epsilon}  floor})$
Depth First Search	no (unless $m < \infty$ )	no	$O(b^m)$	O(bm)
Depth-Limited Search	no (unless $d < maxdepth$ )	no	$O(b^{maxdepth})$	$O(b \cdot maxdepth)$
Iterative Deepening	yes	no	$O(b^d)$	O(bd)
Search		(unless $c = 1$ )		



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## Uniform Cost Search / Explicit branch bookkeeping

```
i uniform-cost-search(X, succ, cost, x_0, g):
                                                                                  1 uniform-cost-search(X, succ, cost, x_0, q):
2 border := \{x_0\}
                                                                                  2 border := \{x_0\}
s c(x_0) := 0
                                                                                  c(x_0) := 0
4 while border \neq \emptyset do
                                                                                  4 while border \neq \emptyset do
          x := \operatorname{argmin}_{x \in \operatorname{border}} c(x)
          if q(x) = 1
                                                                                            if q(x) = 1
6
             return x
7
                                                                                            fi
8
          for y \in succ(x, A) do
9
               border := border \cup \{y\}
10
                                                                                 10
               c(y) := c(x) + \cot(x, y)
11
                                                                                 11
           od
12
                                                                                 12
           border := border \setminus \{x\}
                                                                                            od
13
                                                                                 13
14 <u>od</u>
                                                                                 14
15 return ∅
                                                                                 15 od
```

If succ is expensive to invert (or not possible to invert, because the search space is not a tree), branches must be stored explicitely.

```
x := \operatorname{argmin}_{x \in \operatorname{border}} c(x)
               return branch(x, previous)
            for y \in \operatorname{succ}(x, A) do
                 border := border \cup \{y\}
                 c(y) := c(x) + \cos(x, y)
                 previous(y) := x
            border := border \setminus \{x\}
16 return ∅
18 branch(x, previous):
19 P := \emptyset
20 while x \neq \emptyset do
            insert-at-beginning(P, x)
21
            x := \operatorname{previous}(x)
22
23 od
24 <u>return</u> P
```



#### Uniform Cost Search / Duplicate states

If duplicate states can occur
(i.e., there are several paths to the same state,
i.e., the search space is not a tree),
and if still a tree search should be applied,
states cannot be used as index anymore,
but have to be wrapped in "nodes".

The same modifications have to be applied to all other search algorithms.

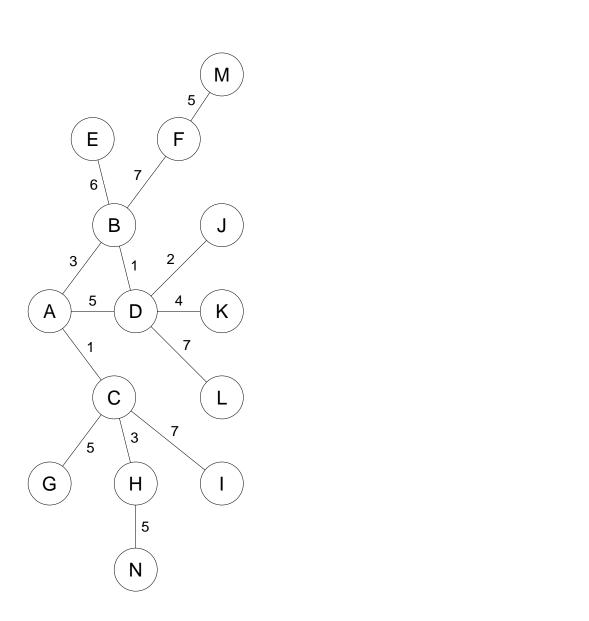


#### Uniform Cost Search / Duplicate states

```
1 uniform-cost-search(X, succ, cost, x_0, g):
                                                                                i uniform-cost-search(X, succ, cost, x_0, g):
 2 border := \{x_0\}
                                                                                2 N := \text{new node}(\text{state} = x_0, c = 0, \text{previous} = \emptyset)
 s c(x_0) := 0
                                                                                s border := \{N\}
 4 while border \neq \emptyset do
                                                                                4 while border \neq \emptyset do
           x := \operatorname{argmin}_{x \in \operatorname{border}} c(x)
                                                                                          N := \operatorname{argmin}_{N \in \operatorname{border}} N.c
 5
           \underline{\mathbf{if}} g(x) = 1
                                                                                          \underline{\mathbf{if}} g(N.\mathsf{state}) = 1
 6
               return branch(x, previous)
                                                                                              <u>return</u> branch(N)
 7
 8
                                                                                8
           for y \in succ(x, A) do
                                                                                           for y \in \text{succ}(N.\text{state}, A) do
 9
                                                                                9
                 border := border \cup \{y\}
                                                                                                N' := \text{new node}(\text{state} = y,
10
                                                                               10
                 c(y) := c(x) + \cos(x, y)
                                                                                                                      c = N.c + cost(N.state, y),
11
                                                                               12
                 previous(y) := x
                                                                                                                      previous := N)
12
                                                                               14
                                                                                               border := border \cup \{N'\}
           od
                                                                               15
13
            border := border \setminus \{x\}
                                                                                           od
14
                                                                               16
                                                                                           border := border \setminus \{N\}
15 od
                                                                               17
16 <u>return</u> ∅
                                                                               18 od
                                                                               19 return ∅
18 branch(x, previous):
                                                                               20
19 P := \emptyset
                                                                               21 branch(N):
20 while x \neq \emptyset do
                                                                              22 P := \emptyset
           insert-at-beginning(P, x)
                                                                              23 while N! = \emptyset do
21
                                                                                          insert-at-beginning(P, N.state)
           x := \operatorname{previous}(x)
22
                                                                               24
                                                                                           N := N.previous
23 od
                                                                               25
24 return P
                                                                               26 <u>od</u>
                                                                               27 return P
```

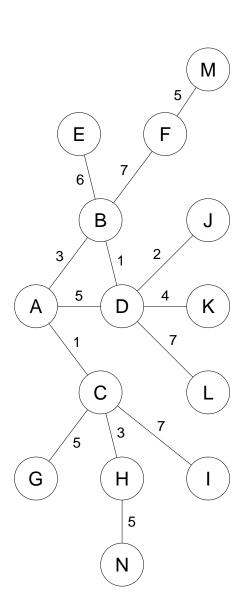


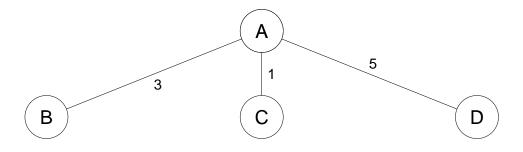
# Several paths blow up the search tree





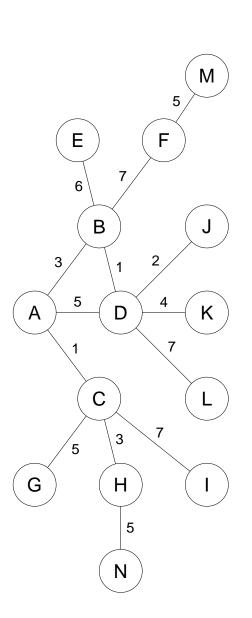
## Several paths blow up the search tree

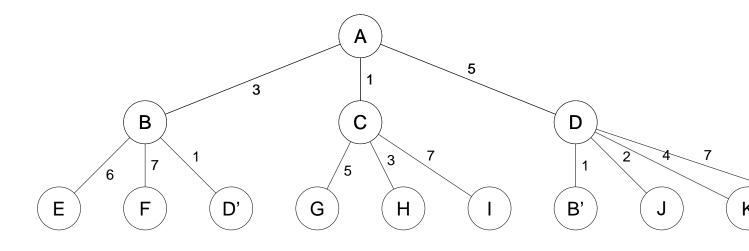






## Several paths blow up the search tree







#### Closed list

The tree search algorithms must be modified s.t. they keep track of all the nodes visited so far (so-called **closed list**).

If the current state is already in the closed list, it is discarded instead of expanded.

This means that all algorithms have to keep the whole visited part of the state space in memory, i.e., the space complexity always is the one of breadth first search..



## Uniform Cost Search in Graph State Spaces (1/2)

```
i uniform-cost-search(X, succ, cost, x_0, g):
                                                                                           i uniform-cost-search-graph(X, succ, cost, x_0, g):
                                                                                           2 visited := \emptyset
 2 border := \{x_0\}
 s c(x_0) := 0
                                                                                           s \text{ border} := \{x_0\}
 4 while border \neq \emptyset do
                                                                                           4 c(x_0) := 0
            x := \operatorname{argmin}_{x \in \operatorname{border}} c(x)
                                                                                           5 while border \neq \emptyset do
            if q(x) = 1
                                                                                                      x := \operatorname{argmin}_{x \in \operatorname{border}} c(x)
 6
                                                                                                      if q(x) = 1
 7
                return x
                                                                                                          return x
8
                                                                                           8
            for y \in \operatorname{succ}(x, A) do
9
                  border := border \cup \{y\}
                                                                                                      \underline{\mathbf{for}}\ y \in \mathrm{succ}(x,A)\ \underline{\mathbf{do}}
10
                                                                                          10
                  c(y) := c(x) + \cos(x, y)
                                                                                                            \underline{\mathbf{if}} \ y \not\in \text{visited}
11
                                                                                         11
                                                                                                               border := border \cup \{y\}
            od
12
                                                                                          12
                                                                                                               c(y) := c(x) + cost(x, y)
            border := border \setminus \{x\}
13
                                                                                         13
                                                                                                               previous(y) := x
14 od
                                                                                          14
15 return ∅
                                                                                                           fi
                                                                                          15
                                                                                          16
                                                                                                      border := border \setminus \{x\}
                                                                                          17
                                                                                                      visited := visited \cup \{x\}
                                                                                          18
                                                                                         19 od
```

20 <u>retu</u>rn Ø



## Uniform Cost Search in Graph State Spaces (2/2)

```
i uniform-cost-search-graph(X, succ, cost, x_0, g):
                                                                                              i uniform-cost-search-graph(X, succ, cost, x_0, g):
2 visited := \emptyset
                                                                                              2 notvisited := X
3 border := \{x_0\}
                                                                                              s c(x) := \begin{cases} 0, & \text{if } x = x_0 \\ \infty, & \text{else} \end{cases} 
c(x_0) := 0
5 while border \neq \emptyset do
                                                                                              4 while notvisited \neq \emptyset do
                                                                                                          x := \operatorname{argmin}_{x \in \operatorname{notvisited}} c(x)
            x := \operatorname{argmin}_{x \in \operatorname{horder}} c(x)
            if q(x) = 1
                                                                                                          \mathbf{if} g(x) = 1
                return x
                                                                                                             return x
 8
9
                                                                                                          for y \in \operatorname{succ}(x, A) do
            for y \in \operatorname{succ}(x, A) do
10
                  if y \notin \text{visited}
                                                                                                               c(y) := c(x) + \cos(x, y)
11
                                                                                             10
                     \mathsf{border} := \mathsf{border} \cup \{y\}
                                                                                                               previous(y) := x
12
                                                                                             11
                     c(y) := c(x) + cost(x, y)
                                                                                                          od
13
                                                                                             12
                     previous(y) := x
                                                                                                          notvisited := notvisited \setminus \{x\}
14
                                                                                             13
                 fi
                                                                                             14 od
15
                                                                                             15 return ∅
16
            border := border \setminus \{x\}
17
            visited := visited \cup \{x\}
18
19 od
20 return ∅
```



#### Summary (1/3) – The Agent Metaphor

- The agent metaphor describes intelligent systems as agents acting in an environment perceived through sensors and remembered as perception sequences from which an action sequence is derived that is executed with actuators.
   Performance measures describe how successful an agent behaves.
- Action tables can describe simple reactive agent behavior.
- Environments can be characterized along many characteristics such as deterministic—stochastic, static—dynamic, fully—partially observable, discrete—continuous.
   episodic—sequential, single—multi agent.



#### Summary (2/3) – Search Problems

- More formally, many AI problems can be described as finding a path in a graph with lowest cost where often (i) the graph is not finite but generated by a successor function and (ii) the goal states are not enumerated explicitly but characterized by a goal test.
- The same problem can be represented more or less nicely as a formal search problem (see 8 queens example).
- The complexity of search problems can be described by the maximum branching factor, depth of least-cost solution and maximum depth of state space, and the (runtime and memory) complexity of search algorithms as function in these characteristics.
- Furthermore algorithms can be characterized by completeness and optimality.



#### Summary (3/3) – Uninformed Search Algorithms

- Breadth-First Search is complete and can be modified to be optimal (Uniform Cost Search). Depth First Search is not complete, but can be modified to be complete (Iterative Deepending Search). BFS suffers from memory complexity, while DFS suffers from time complexity.
- If the search space is not a tree, but a general graph, a closed list of all already visited states needs to be maintained.