Bayesian Networks - Exercise Sheet 1

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April 21, 2015

Solutions need to be handed in until Monday, April 27th, 2013 at 12:00

Exercise 1: Events and Conditional Probabilities (12P)

a) Consider two distinguishable dices that are being rolled simultaneously. Let $\Omega := \{1, ..., 6\}^2$ be the event space of all (i, j) tuples. Let $X : \Omega \to \mathbb{N}$ be a random variable defined by:

$$X:(i,j)\mapsto i+j$$

For the upcoming examples, write down their set of elementary events (all $e \in \Omega$) and compute the probability. Note that not all events need to involve X.

- \bullet A: Rolling the same number twice
- *B* : *X* < 4
- $C: X \leq 4$
- \bullet D:X is an even number
- \bullet E: The first dice shows the number 2

Now compute the following conditional probabilities:

- P(D|A) and P(A|D)
- P(C|A) and P(A|C)
- P(E|C) and P(C|E)
- ullet Are A and C conditionally independent given B? Explain your answer in detail.
- b) A Skat Game consists of 16 red cards (hearts, diamonds) and 16 black cards (spades, clubs). Of every color there are 8 cards which are in descending order ace, king, queen, jack, 10, 9, 8, 7. Let the event A denote drawing an ace out of a full stack of cards. Your friend Tom draws cards and gives hints. Do the hints help in deducing if he drew an ace? Explain your answers in detail.
 - Tom draws a card and says it is of clubs.

- Tom draws a card and says it is not a queen.
- Tom draws a card and says it is red.
- Tom draws a card and says the card is lower than a jack.

Exercise 2: Marginalizing a Joint Probability Distribution (8P)

The cold is an annoying disease and has very many symptoms. Three of these symptoms are *nausea*, a *sore throat* and a *headache*. In the table below, there are the results of 280 patients.

- a) Copy the table from below and write down the relative probabilities, i.e. make a table of the joint probability distribution P(C, N, S, H).
- b) Write down the following marginal distributions P(N), P(S) and P(H).
- c) How many patients were suffering from a cold but did not suffer from headaches?

	Sore Throat	Yes						No				
	Nausea	Yes			No			Yes		No		
	Headache	Yes		No	Yes	N	0	Yes	No	Yes	- 1	No
Cold	Yes		67	1	2	3	37	25	3		1	1
	No		2		5	6	17	12	20	1	4	55