Exercise Sheet SoSe 2015
Wirtschaftsinformatik und Maschinelles Lernen (ISMLL)
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## Exercise Sheet Computer Vision 5

Submission: 10.6
(3 Points)

## Exercise 1 DLT (20 Points)

a) Given following points, extracted from two images with SURF feature detector and extractor, use the classic DLT algorithm to compute the homography transformation matrix $H$. Show all your steps dumping the matrices to video after each iteration.

| $\mathbf{x}(\mathbf{x}, \mathbf{y}, \mathbf{1})$ | $\mathbf{x}^{\prime}\left(\mathbf{x}^{\mathbf{\prime}}, \mathbf{y}^{\mathbf{\prime}}, \mathbf{1}\right)$ |
| :---: | :---: |
| $(974.64,84.79)$ | $(1010.37,81.95)$ |
| $(1002.11,81.85)$ | $(1151.48,75.10)$ |
| $(938.91,60.76)$ | $(973.68,58.05)$ |
| $(940.81,55.39)$ | $(975.28,52.61)$ |
| $(982.48,48.33)$ | $(1018.36,53.09)$ |

Table 1: points
Useful methods in OpenCV:

- Objects of type Mat should be declared of type attribute CvType.CV_64F
- To multiply 2 matrices: Core.gemm(...);
- To plot a Matrix: Matname.dump();
- To transpose a matrix: Matname.t();
- To compute the SVD: Core.SVDecomp(src, w, u, vt): src decomposed matrix, w calculated singular values, u calculated left singular vectors, vt transposed matrix of right singular values;

Hint: Pay attention to matrix dimensionalities.
(10 Points)
b) How should the code be modified to use the normalized DLT algorithm? Explain how the normalization matrices are computed and how and when this normalizations is applied to the data. Why is the normalization important?
(5 Points)
c) Apply gradient descent on the function $f(x)=\frac{1}{4} x^{4}+\frac{1}{3} x^{3}-\frac{1}{2} x^{2}$ with following configurations:

- Use step length $\mathrm{a}=0.3$ and starting point $\mathrm{x} 0=-1$ and show the first four iterations. What is your minimum?
- Use step length $\mathrm{a}=2$ and starting point $\mathrm{x} 0=-1$ and show the first four iterations. What has happened and why?
- Use step length $\mathrm{a}=0.3$ and starting point $\mathrm{x} 0=0$ and show the first two iterations. What has happened and why? Do the same again with $\mathrm{a}=0.8$ and starting point $\mathrm{x} 0=0.5$ and show the first four iterations. Where is your minimum now?
(5 Points)

