# Machine Learning <br> Exercise Sheet 9 

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## Exercise 17: Constraint Optimization with Lagrange Multipliers (5 Points)

a) Minimize the function $f(x, y)=(x+y)^{2}$ subject to $-3 x+y=-1$. What are all feasible minima?
b) Maximize the function $g(x)=2 x^{3}-3 x$ subject to $x \leq 0.5$. What are all feasible maxima?

## Exercise 18: SVM (5 Points)

| $x_{1}$ | $x_{2}$ | $y$ | $\alpha_{i}$ |
| :---: | :---: | :---: | :---: |
| -1 | 0 | 1 | 1 |
| 0 | 0 | -1 | 1 |
| 1 | 0 | -1 | 0 |
| -1 | -1 | 1 | 0 |
| 0 | -1 | 1 | 1 |
| 1 | -1 | -1 | $1 / 3$ |
| -0.5 | -0.5 | -1 | $2 / 3$ |

a) Give a pseudo code that summarizes how an SVM is learned using SMO.
b) Read (at least) section 12.2 .2 of the SMO Book. Explain the heuristic for choosing which multipliers to optimize in your own words.
c) Classify all instances in the table above using an SVM with the given $\alpha$ and $b=1$.
d) Plot the data and add the decision boundary of the SVM. Which are the support vectors?

