Modern Optimization Techniques - Exercise Sheet 11

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Solutions need to be handed in until Monday, February 05, 2018 at 10:00

Exercise 1: Barrier Methods in General (10P)

- a) Explain in your own words how the barrier method works for a general constrained minimization problem!
- b) Consider the simple optimization problem:

minimize
$$x^2 + 1$$

subject to $x \in [2, 4]$

Plot $tf_0(x) + \phi(x)$ for values of t = 1, 5, 10, 20. Label $x^*(t)$ in your plots. Does it converge (in the sense of t) to the minimizer of the original problem?

c) Derive the dual feasible pair $\lambda^*(t), \nu^*(t)$ if instead h(u) = -1/u is used in the definition of barrier function

$$\phi(x) = \sum_{i=1}^{m} h(f_i(x))$$

Exercise 2: Applying the Barrier Method (10P)

What happens if the barrier method is applied to the following optimization problem:

minimize
$$x_2$$

subject to $x_1 \le x_2$
 $0 \le x_2$

Formulate the optimization problem into the standard form to then write down the derived optimization problem. Solve it by using a Newton step as centering step. Start in the feasible point x=(-0.5,1), use a step size of $\mu=0.05$ and t=10. Plot the iterates and explain what is happening.